Mata Matters: Using views onto the data

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Abstract. Mata is Stata’s matrix language. In the Mata Matters column, we show how Mata can be used interactively to solve problems and as a programming language to add new features to Stata. In this issue’s column, we explore view matrices, matrices that are views of the underlying Stata dataset rather than copies of it.

Keywords: pr0019, Mata, views, memory

Overview

A data matrix is a matrix in which the rows are observations and the columns are variables. For instance, say we have the following data in Stata:

```
. list
  mpg weight displa-t
1. 22 2930 121
2. 17 3350 258
3. 22 2640 121
4. 20 3250 196
5. 15 4080 350
```

In Mata, we can obtain a copy of the data by typing

```
. mata:
    mata (type end to exit) -----
    : X = st_data(., .)
    : X

    1  2  3
    1  22 2930 121
    2  17 3350 258
    3  22 2640 121
    4  20 3250 196
    5  15 4080 350
```

The data matrix we have just created might be used subsequently in the matrix formula \( \mathbf{b} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y} \), for some vector \( \mathbf{y} \).

What is important to understand about the above is that \( \mathbf{X} \) is a copy. If we were to modify the dataset, or even drop it, that would not change \( \mathbf{X} \). If we were to modify \( \mathbf{X} \), or even drop it, that would not change the dataset.
Function \texttt{st\_view()} provides an alternative to \texttt{st\_data()} for accessing the data stored in the Stata dataset.

\begin{verbatim}
: st_view(V=., ., .)
: V

\begin{tabular}{ccc}
  1 & 2 & 3 \\
  1 & 22 & 2930 & 121 \\
  2 & 17 & 3350 & 258 \\
  3 & 22 & 2640 & 121 \\
  4 & 20 & 3250 & 196 \\
  5 & 15 & 4080 & 350 \\
\end{tabular}
\end{verbatim}

\(V\) has the same contents as \(X\) and can be used in the same way. For instance, we might subsequently calculate \((V'V)^{-1}V'y\). The difference between \(X\) and \(V\) is that \(V\) is a view: matrix \(V\) and the Stata dataset are the same. If we were to modify \(V\), the dataset would change:

\begin{verbatim}
: V[1,1] = 500
: end

. list

<table>
<thead>
<tr>
<th></th>
<th>mpg</th>
<th>weight</th>
<th>displa-t</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>500</td>
<td>2,930</td>
<td>121</td>
</tr>
<tr>
<td>2.</td>
<td>17</td>
<td>3,350</td>
<td>258</td>
</tr>
<tr>
<td>3.</td>
<td>22</td>
<td>2,640</td>
<td>121</td>
</tr>
<tr>
<td>4.</td>
<td>20</td>
<td>3,250</td>
<td>196</td>
</tr>
<tr>
<td>5.</td>
<td>15</td>
<td>4,080</td>
<td>350</td>
</tr>
</tbody>
</table>
\end{verbatim}

Similarly, if we were to modify the dataset, \(V\) would change:

\begin{verbatim}
. replace mpg = 2 in 1
(1 real change made)
. mata:
: mata (type end to exit) ----
: V

\begin{tabular}{ccc}
  1 & 2 & 3 \\
  1 & 2 & 2930 & 121 \\
  2 & 17 & 3350 & 258 \\
  3 & 22 & 2640 & 121 \\
  4 & 20 & 3250 & 196 \\
  5 & 15 & 4080 & 350 \\
\end{tabular}
\end{verbatim}

The other difference is in the amount of memory consumed by \(V\) and \(X\):
Both matrices are 5 \times 3, but \texttt{X}, being a copy, consumes 5 \times 3 \times 8 = 120 \text{ bytes}, whereas \texttt{V}, being a view, consumes only 16 \text{ bytes}. The difference, 120 - 16 = 104 \text{ bytes}, is not much, but were the matrices larger, the difference would become larger, too.

Let's assume we have a 100,000 \times 3 dataset. Then here is what we would see:

\begin{verbatim}
: X = st_data(., .)
: st_view(V=., ., .)
: mata describe

# bytes type name and extent
---
16  real matrix     V[100000,3]
2,400,000  real matrix     X[100000,3]
\end{verbatim}

\texttt{X}, our copy, would have taken 100,000 \times 3 \times 8 = 2,400,000 \text{ bytes}. \texttt{V}, our view, would still have taken only 16 \text{ bytes}. Now there is a difference of 2,399,984 \text{ bytes}.

Memory savings is the most important reason to use views. Data matrices are usually the largest matrices in matrix calculations, and it is often convenient to have more than one. With views, it does not matter how many matrices you have.

Most views take more than 16 \text{ bytes}, but they never take much, especially in comparison with a copy. So far, we have included all the variables and all the observations. If we select some variables and omit others, a little more memory will be required—4 \text{ bytes} per variable selected in the worst case, and sometimes fewer.

If we omit some observations and include others, we will similarly face a 4-byte-per-included-observation cost in the worst case, and just as with variables, sometimes it will be fewer.

Although memory savings is the most important feature of views, I will show that the ability to change the matrix and change the underlying data can also be put to good use.

**Selecting subsets**

The basic recipe for creating a view is

\begin{verbatim}
st_view(V=., ., .)
\end{verbatim}

where you substitute for \texttt{V} the name of the matrix you wish to create. Do not get hung up on how odd the first argument, \texttt{V=}, looks. Just change \texttt{V} to the name of your matrix or, if you prefer, you can type
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\[ V\text{=}.
\text{st\_view}(V, ., .)\]

You must code \( V\text{=}\) one way or the other because the arguments to \texttt{st\_view()} must already exist, just as for any function. The real question is not why you have to code \( V\text{=}\) so much as why the syntax is not \( V = \texttt{st\_view}(., .)\). That is because matrix \( V \) will be special and \texttt{st\_view()} must lay its hands on \( V \) to make it special. In the process, it does not matter what \( V \) contained because \texttt{st\_view()} re-creates it. When \( V \) already exists, you can dispense with the \( V\text{=}\) if you wish. You can also dispense with the preassignment when writing code within Mata programs. In both cases, it does not matter which you do.

In any case, the odd-looking first argument \( V\text{=}\) specifies the matrix to be created. The second argument specifies the observations to be included, and the third argument specifies the variables. Specifying the second argument as \( .\) means to include all observations. Specifying the third argument as \( .\) means to include all variables.

Usually, in interactive use, you will want all the observations, but it is rare that you will want all the variables. Let’s assume that, using the auto data, we wish to calculate

\[ b = (X'X)^{-1}X'y \]

for

\[ y = (\text{mpg}) \]
\[ X = (\text{weight}, \text{foreign}, 1) \]

The solution using views is

\[ . \text{sysuse auto, clear} \]
\[ . \text{(1978 Automobile Data)} \]
\[ . \text{gen one = 1} \]
\[ . \text{mata:} \]
\[ . \text{st\_view(y=., ., "mpg")} \]
\[ . \text{st\_view(X=., ., ("weight", "foreign", "one"))} \]
\[ . b = \text{invsym(X'X)}*X'y \]
\[ . b \]
\[ 1 -0.0065878864 \]
\[ 2 -1.650029106 \]
\[ 3 41.67970233 \]

\[ : \text{end} \]
Note the two calls to `st_view()`. To create `y`, we specified the third argument as "mpg". To create `X`, we specified the third argument as ("weight", "foreign", "one"). The third argument specifies the variables to be selected, and the argument is specified as a row vector of names.

Once the view matrices are created, we use them just as we would any matrix. The bulk of the calculation is

\[ b = \text{invsym}(X'X)X'y \]

whether `X` and `y` are views or copies. And, whether `X` and `y` are views or copies, it would be better if the calculation were coded as

\[ b = \text{invsym}(\text{cross}(X,X))\text{cross}(X,y) \]

because function `cross()` is more accurate, faster, and uses less memory than multiplication in these sorts of situations; see [M-5] `cross()`. This detail has nothing to do with these discussions, but both the numerical analyst and the programmer in me demand that I mention that.

### Missing values

In calculations like \( b = (X'X)^{-1}X'y \), missing values will result in missing results. Had there been any missing values in the data, the final result would have been

```
: b
     1
  1 .
  2 .
  3 .
```

Let us assume that we wish simply to ignore observations that contain missing values. The easiest way is to drop any observations containing them before creating the views. In Stata, there are many ways of finding and eliminating observations that contain missing values. I use the following,

```
. egen missing = rowmiss(mpg weight foreign)
. drop if missing
```

and so our solution would become

```
. sysuse auto, clear
. gen one = 1
. egen missing = rowmiss(mpg weight foreign)
. drop if missing
. mata:
    : st_view(y=., ., "mpg")
    : st_view(X=., ., ("weight", "foreign", "one"))
    : b = invsym(X'X)*X'y
    : end
```
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That, however, is not the solution I would choose in a programming context. \texttt{st_view()} allows an optional fourth argument in which you can specify the name of a variable that marks the observations to be included, which is often called a \texttt{touse} variable. In a programming context, I would create a \texttt{touse} variable in the standard way—\texttt{touse} variables contain nonzero for observations to be used and zero for observations to be omitted—and then I would specify that variable’s name as the fourth argument. Do not get hung up on this because the point of this column is interactive use, but I do want to show programmers how this would be done:

```st_view()
```

Using views to replace values in the dataset

When you replace a value in a view, you also change the value in the underlying Stata dataset. This feature can be useful in data-management problems.

Say you have a dataset containing the variables \texttt{stat72}, \texttt{stat73}, \ldots, \texttt{stat99} that record a patient’s status in 1972, 1973, \ldots, 1999. You wish to add new variable \texttt{firstyear} recording the first year in which a status variable takes on the value 1.

The standard solution to this problem involves reshaping the data to long form, using standard commands to fill in variable \texttt{firstyear}, and reshaping the data back to wide form.
Here is another solution:

. gen byte firstyear = .
. mata:
: names = "stat72 stat73 stat74 stat75 stat76 stat77 stat78 stat79
        stat80 stat81 stat82 stat83 stat84 stat85 stat86 stat87 stat88 stat89
        stat90 stat91 stat92 stat93 stat94 stat95 stat96 stat97 stat98 stat99"
: st_view(s=., ., tokens(names))
: st_view(first=., ., "firstyear")
: for (i=1; i<=rows(s); i++) {
    for (j=1; j<=cols(s); j++) {
        if (s[i,j]==1) {
            first[i] = j+71 /* <- note this line */
            break
        }
    }
}
: end

In this program, we use two views.

s is a view onto variables stat72, stat73, ..., stat99. That makes it easy to loop over the variables.

first is a view onto variable firstyear. Notice the marked line in the midst of the for loops: first[i] = j+71. When we change first, we change firstyear.

About the Author

William Gould is President of StataCorp, head of development, and principal architect of Mata.